

nag_regsn_mult_linear_upd_model (g02ddc)

1. Purpose

nag_regsn_mult_linear_upd_model (g02ddc) calculates the regression parameters for a general linear regression model. It is intended to be called after `nag_regsn_mult_linear_addrem_obs (g02dcc)`, `nag_regsn_mult_linear_add_var (g02dec)` or `nag_regsn_mult_linear_delete_var (g02dfc)`.

2. Specification

```
#include <nag.h>
#include <nagg02.h>

void nag_regsn_mult_linear_upd_model(Integer n, Integer ip, double q[],
    Integer tdq, double *rss, double *df, double b[], double se[],
    double cov[], Boolean *svd, Integer *rank, double p[], double tol,
    NagError *fail)
```

3. Description

A general linear regression model fitted by `nag_regsn_mult_linear (g02dac)` may be adjusted by adding or deleting an observation using `nag_regsn_mult_linear_addrem_obs (g02dcc)`, adding a new independent variable using `nag_regsn_mult_linear_add_var (g02dec)` or deleting an existing independent variable using `nag_regsn_mult_linear_delete_var (g02dfc)`. These functions compute the vector c and the upper triangular matrix R . `nag_regsn_mult_linear_upd_model` takes these basic results and computes the regression coefficients, $\hat{\beta}$, their standard errors and their variance-covariance matrix.

If R is of full rank, then $\hat{\beta}$ is the solution to:

$$R\hat{\beta} = c_1,$$

where c_1 is the first p elements of c .

If R is not of full rank a solution is obtained by means of a singular value decomposition (SVD) of R ,

$$R = Q_* \begin{pmatrix} D & 0 \\ 0 & 0 \end{pmatrix} P^T$$

where D is a k by k diagonal matrix with non-zero diagonal elements, k being the rank of R , and Q_* and P are p by p orthogonal matrices. This gives the solution

$$\hat{\beta} = P_1 D^{-1} Q_{*1}^T c_1$$

P_1 being the first k columns of P , i.e., $P = (P_1 P_0)$ and Q_{*1} being the first k columns of Q_* .

Details of the SVD, are made available, in the form of the matrix P^* :

$$P^* = \begin{pmatrix} D^{-1} P_1^T \\ P_0^T \end{pmatrix}$$

This will be only one of the possible solutions. Other estimates may be obtained by applying constraints to the parameters. These solutions can be obtained by calling `nag_regsn_mult_linear_tran_model (g02dkc)` after calling `nag_regsn_mult_linear_upd_model`. Only certain linear combinations of the parameters will have unique estimates, these are known as estimable functions. These can be estimated using `nag_regsn_mult_linear_est_func (g02dnc)`.

The residual sum of squares required to calculate the standard errors and the variance-covariance matrix can either be input or can be calculated if additional information on c for the whole sample is provided.

4. Parameters

n

Input: number of observations.
 Constraint: $n \geq 1$.

ip

Input: the number of terms in the regression model, p .
 Constraint: $ip \geq 1$.

q[n][tdq]

Input: **q** must be the array **q** as output by nag_regsn_mult_linear_addrem_obs (g02dcc), nag_regsn_mult_linear_add_var (g02dec) or nag_regsn_mult_linear_delete_var (g02dfc). If on entry $rss \leq 0.0$ then all **n** elements of c are needed. This is provided by functions nag_regsn_mult_linear_add_var (g02dec) or nag_regsn_mult_linear_delete_var (g02dfc).

tdq

Input: **tdq** the last dimension of the array **q** as declared in the function from which nag_regsn_mult_linear_upd_model is called.
 Constraint: $tdq \geq ip+1$.

rss

Input: either the residual sum of squares or a value less than or equal to 0.0 to indicate that the residual sum of squares is to be calculated by the function.
 Output: if $rss \leq 0.0$ on entry, then on exit **rss** will contain the residual sum of squares as calculated by nag_regsn_mult_linear_upd_model.

If **rss** was positive on entry, then it will be unchanged.

df

Output: the degrees of freedom associated with the residual sum of squares.

b[ip]

Output: the estimates of the p parameters, $\hat{\beta}$.

se[ip]

Output: the standard errors of the p parameters given in **b**.

cov[ip*(ip+1)/2]

Output: the upper triangular part of the variance-covariance matrix of the p parameter estimates given in **b**. They are stored packed by column, i.e., the covariance between the parameter estimate given in $b[i]$ and the parameter estimate given in $b[j]$, $j \geq i$, is stored in $cov[j(j+1)/2 + i]$, for $i = 0, 1, \dots, ip - 1$ and $j = i, i + 1, \dots, ip - 1$.

svd

Output: if a singular value decomposition has been performed, then **svd** = **TRUE**, otherwise **svd** = **FALSE**.

rank

Output: the rank of the independent variables.

If **svd** = **FALSE**, then **rank** = **ip**.

If **svd** = **TRUE**, then **rank** is an estimate of the rank of the independent variables.

rank is calculated as the number of singular values greater than $tol \times$ (largest singular value).

It is possible for the singular value decomposition to be carried out but **rank** to be returned as **ip**.

p[ip*ip+2*ip]

Output: **p** contains details of the singular value decomposition if used.

If **svd** = **FALSE**, **p** is not referenced.

If **svd** = **TRUE**, the first **ip** elements of **p** will not be referenced, the next **ip** values contain the singular values. The following **ip*ip** values contain the matrix P^* stored by rows.

tol

Input: the value of **tol** is used to decide if the independent variables are of full rank and, if not, what is the rank of the independent variables. The smaller the value of **tol** the stricter the criterion for selecting the singular value decomposition. If **tol** = 0.0, then the singular

value decomposition will never be used, this may cause run time errors or inaccuracies if the independent variables are not of full rank.

Suggested value: **tol** = 0.000001.

Constraint: **tol** \geq 0.0.

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library.

5. Error Indications and Warnings

NE_INT_ARG_LT

On entry, **n** must not be less than 1: **n** = $\langle value \rangle$.

On entry, **ip** must not be less than 1: **ip** = $\langle value \rangle$.

NE_2_INT_ARG_LT

On entry **tdq** = $\langle value \rangle$ while **ip** + 1 = $\langle value \rangle$. These parameters must satisfy **tdq** \geq **ip** + 1.

On entry, **n** = $\langle value \rangle$ while **ip** = $\langle value \rangle$. These parameters must satisfy **n** \geq **ip**.

NE_DOF_LE_ZERO

The degrees of freedom for error are less than or equal to 0. In this case the estimates, $\hat{\beta}$, are returned but not the standard errors or covariances.

NE_SVD_NOT_CONV

The singular value decomposition has failed to converge.

NE_REAL_ARG_LT

On entry, **tol** must not be less than 0.0: **tol** = $\langle value \rangle$.

NE_ALLOC_FAIL

Memory allocation failed.

6. Further Comments

6.1. Accuracy

The accuracy of the results will depend on the accuracy of the input *R* matrix, which may lose accuracy if a large number of observations or variables have been dropped.

6.2. References

Golub G H and Van Loan C F (1983) *Matrix Computations* Johns Hopkins University Press, Baltimore.

Hammarling S (1985) The Singular Value Decomposition in Multivariate Statistics *ACM Signum Newsletter* **20** (3) 2–25.

Searle S R (1971) *Linear Models* Wiley.

7. See Also

nag_regsn_mult_linear (g02dac)
 nag_regsn_mult_linear_addrem_obs (g02dcc)
 nag_regsn_mult_linear_add_var (g02dec)
 nag_regsn_mult_linear_delete_var (g02dfc)
 nag_regsn_mult_linear_tran_model (g02dkc)
 nag_regsn_mult_linear_est_func (g02dnc)

8. Example

A data set consisting of 12 observations and four independent variables is input and a regression model fitted by calls to nag_regsn_mult_linear_add_var (g02dec). The parameters are then calculated by nag_regsn_mult_linear_upd_model and the results printed.

8.1. Program Text

```

/* nag_regsn_mult_linear_upd_model(g02ddc) Example Program
 *
 * Copyright 1991 Numerical Algorithms Group.
 *
 * Mark 2, 1991.
 */
#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagg02.h>

#define NMAX 12
#define MMAX 5
#define TDX MMAX
#define TDQ MMAX+1

main()
{
    double  rss, tol;
    Integer i, ip, rank, j, m, n;
    double  df;
    Boolean svd;
    char    weight;
    double  b[MMAX], cov[MMAX*(MMAX+1)/2], p[MMAX*(MMAX+2)],
    q[NMAX][MMAX+1], se[MMAX], wt[NMAX], x[NMAX][MMAX], xe[NMAX];
    double  *wtptr;
    static  NagError fail;

    Vprintf("g02ddc Example Program Results\n");
    /* Skip heading in data file */
    Vscanf("%*[^\\n]");
    Vscanf("%ld %ld %c", &n, &m, &weight);
    if (weight=='w')
        wtptr = wt;
    else
        wtptr = (double *)0;

    if (n<=NMAX && m<MMAX)
    {
        if (wtptr)
        {
            for (i=0; i<n; i++)
            {
                for (j=0; j<m; j++)
                    Vscanf("%lf", &x[i][j]);
                Vscanf("%lf%lf", &q[i][0], &wt[i]);
            }
        }
        else
        {
            for (i=0; i<n; i++)
            {
                for (j=0; j<m; j++)
                    Vscanf("%lf", &x[i][j]);
                Vscanf("%lf", &q[i][0]);
            }
        }
        /* Set tolerance */
        tol = 0.000001e0;
        ip = 0;
        for (j=0; j<m; ++j)
        {
            /*
             *          Fit model using g02dec
             */
            for (i=0; i<n; i++)
                xe[i] = x[i][j];
            g02dec(n, ip, (double *)q, (Integer)(TDQ), p, wtptr, xe, &rss,

```

```

        tol, &fail);
    if (fail.code==NE_NOERROR)
        ip += 1;
    else if (fail.code==NE_NVAR_NOT_IND)
        Vprintf(" * New variable not added * \n");
    else
    {
        Vprintf("%s\n", fail.message);
        exit(EXIT_FAILURE);
    }
}
rss = 0.0;
g02ddc(n, ip, (double *)q, (Integer)(TDQ), &rss, &df, b, se, cov, &svd,
        &rank, p, tol, NAGERR_DEFAULT);

Vprintf("\n");
if (svd)
    Vprintf("Model not of full rank\n\n");
Vprintf("Residual sum of squares = %12.4e\n", rss);
Vprintf("Degrees of freedom = %3.1f\n\n", df);
Vprintf("Variable   Parameter estimate   Standard error\n\n");
for (j=0; j<ip; j++)
    Vprintf("%6ld%20.4e%20.4e\n", j+1, b[j], se[j]);
Vprintf("\n");
}
else
{
    Vfprintf(stderr, "One or both of m and n are out of range:\n
m = %-3ld while n = %-3ld\n", m, n);
    exit(EXIT_FAILURE);
}
exit(EXIT_SUCCESS);
}

```

8.2. Program Data

```

g02ddc Example Program Data
 12 4 u
1.0 0.0 0.0 0.0 33.63
0.0 0.0 0.0 1.0 39.62
0.0 1.0 0.0 0.0 38.18
0.0 0.0 1.0 0.0 41.46
0.0 0.0 0.0 1.0 38.02
0.0 1.0 0.0 0.0 35.83
0.0 0.0 0.0 1.0 35.99
1.0 0.0 0.0 0.0 36.58
0.0 0.0 1.0 0.0 42.92
1.0 0.0 0.0 0.0 37.80
0.0 0.0 1.0 0.0 40.43
0.0 1.0 0.0 0.0 37.89

```

8.3. Program Results

```
g02ddc Example Program Results
```

```
Residual sum of squares = 2.2227e+01
Degrees of freedom = 8.0
```

Variable	Parameter estimate	Standard error
1	3.6003e+01	9.6235e-01
2	3.7300e+01	9.6235e-01
3	4.1603e+01	9.6235e-01
4	3.7877e+01	9.6235e-01